

# Important Motion in Bodies Hanging by String Formulas PDF



Formulas  
Examples  
with Units

List of 15  
Important Motion in Bodies Hanging by String  
Formulas

## 1) Body Lying on Rough Horizontal Plane Formulas ↗

### 1.1) Acceleration of System with Bodies One Hanging Free and Other Lying on Rough Horizontal Plane Formula ↗

Formula

$$a_s = \frac{m_1 - \mu_{hs} \cdot m_2}{m_1 + m_2} \cdot [g]$$

Example with Units

$$5.9401 \text{ m/s}^2 = \frac{29 \text{ kg} - 0.24 \cdot 13.52 \text{ kg}}{29 \text{ kg} + 13.52 \text{ kg}} \cdot 9.8066 \text{ m/s}^2$$

Evaluate Formula ↗

### 1.2) Tension in String given Coefficient of Friction of Horizontal Plane Formula ↗

Formula

$$T_{st} = (1 + \mu_{hor}) \cdot \frac{m_1 \cdot m_2}{m_1 + m_2} \cdot [g]$$

Evaluate Formula ↗

Example with Units

$$130.0352 \text{ N} = (1 + 0.438) \cdot \frac{29 \text{ kg} \cdot 13.52 \text{ kg}}{29 \text{ kg} + 13.52 \text{ kg}} \cdot 9.8066 \text{ m/s}^2$$

## 2) Body Lying on Rough Inclined Plane Formulas ↗

### 2.1) Acceleration of System with Bodies One Hanging Free, Other Lying on Rough Inclined Plane Formula ↗

Formula

$$a_i = \frac{m_1 - m_2 \cdot \sin(\theta_p) - \mu_{hs} \cdot m_2 \cdot \cos(\theta_p)}{m_1 + m_2} \cdot [g]$$

Evaluate Formula ↗

Example with Units

$$5.2463 \text{ m/s}^2 = \frac{29 \text{ kg} - 13.52 \text{ kg} \cdot \sin(13.23^\circ) - 0.24 \cdot 13.52 \text{ kg} \cdot \cos(13.23^\circ)}{29 \text{ kg} + 13.52 \text{ kg}} \cdot 9.8066 \text{ m/s}^2$$



## 2.2) Coefficient of Friction given Frictional Force Formula

Formula

$$\mu_{hs} = \frac{F_{fri}}{m_2 \cdot [g] \cdot \cos(\theta_p)}$$

Example with Units

$$0.24 = \frac{30.97607\text{N}}{13.52\text{kg} \cdot 9.8066\text{m/s}^2 \cdot \cos(13.23^\circ)}$$

Evaluate Formula 

## 2.3) Coefficient of Friction given Tension Formula

Formula

$$\mu_{hs} = \frac{m_1 + m_2}{m_1 \cdot m_1 \cdot [g]} \cdot T_{st} \cdot \sec(\theta_b) - \tan(\theta_b) - \sec(\theta_b)$$

Evaluate Formula 

Example with Units

$$0.2461 = \frac{29\text{kg} + 13.52\text{kg}}{29\text{kg} \cdot 29\text{kg} \cdot 9.8066\text{m/s}^2} \cdot 130\text{N} \cdot \sec(327.5^\circ) - \tan(327.5^\circ) - \sec(327.5^\circ)$$

## 2.4) Frictional Force Formula

Formula

$$F_{fri} = \mu_{hs} \cdot m_2 \cdot [g] \cdot \cos(\theta_p)$$

Evaluate Formula 

Example with Units

$$30.9761\text{N} = 0.24 \cdot 13.52\text{kg} \cdot 9.8066\text{m/s}^2 \cdot \cos(13.23^\circ)$$

## 2.5) Inclination of Plane for given Frictional Force Formula

Formula

$$\theta_p = \arccos\left(\frac{F_{fri}}{\mu_{hs} \cdot m_2 \cdot [g]}\right)$$

Example with Units

$$13.23^\circ = \arccos\left(\frac{30.97607\text{N}}{0.24 \cdot 13.52\text{kg} \cdot 9.8066\text{m/s}^2}\right)$$

Evaluate Formula 

## 2.6) Mass of Body B given Frictional Force Formula

Formula

$$m_2 = \frac{F_{fri}}{\mu_{hs} \cdot [g] \cdot \cos(\theta_p)}$$

Example with Units

$$13.52\text{kg} = \frac{30.97607\text{N}}{0.24 \cdot 9.8066\text{m/s}^2 \cdot \cos(13.23^\circ)}$$

Evaluate Formula 

## 2.7) Tension in String given Coefficient of Friction of Inclined Plane Formula

Formula

$$T_{st} = \frac{m_1 \cdot m_2}{m_1 + m_2} \cdot [g] \cdot (1 + \sin(\theta_p) + \mu_{hs} \cdot \cos(\theta_p))$$

Evaluate Formula 

Example with Units

$$132.2499\text{N} = \frac{29\text{kg} \cdot 13.52\text{kg}}{29\text{kg} + 13.52\text{kg}} \cdot 9.8066\text{m/s}^2 \cdot (1 + \sin(13.23^\circ) + 0.24 \cdot \cos(13.23^\circ))$$



### 3) Body Lying on Smooth Horizontal Plane Formulas

#### 3.1) Acceleration in System Formula

Formula

$$a_b = \frac{m_1}{m_1 + m_2} \cdot [g]$$

Example with Units

$$6.6884 \text{ m/s}^2 = \frac{29 \text{ kg}}{29 \text{ kg} + 13.52 \text{ kg}} \cdot 9.8066 \text{ m/s}^2$$

Evaluate Formula 

#### 3.2) Tension in String if only One Body is Freely Suspended Formula

Formula

$$T_{fs} = \frac{m_1 \cdot m_2}{m_1 + m_2} \cdot [g]$$

Example with Units

$$90.4278 \text{ N} = \frac{29 \text{ kg} \cdot 13.52 \text{ kg}}{29 \text{ kg} + 13.52 \text{ kg}} \cdot 9.8066 \text{ m/s}^2$$

Evaluate Formula 

### 4) Body Lying on Smooth Inclined Plane Formulas

#### 4.1) Acceleration of System with Bodies One Hanging Free and Other Lying on Smooth Inclined Plane Formula

Formula

$$a_s = \frac{m_1 - m_2 \cdot \sin(\theta_p)}{m_1 + m_2} \cdot [g]$$

Evaluate Formula 

Example with Units

$$5.9748 \text{ m/s}^2 = \frac{29 \text{ kg} - 13.52 \text{ kg} \cdot \sin(13.23^\circ)}{29 \text{ kg} + 13.52 \text{ kg}} \cdot 9.8066 \text{ m/s}^2$$

#### 4.2) Angle of Inclination given Acceleration Formula

Formula

$$\theta_p = \arcsin\left(\frac{m_1 \cdot [g] - m_1 \cdot a_s - m_2 \cdot a_s}{m_2 \cdot [g]}\right)$$

Evaluate Formula 

Example with Units

$$13.8881^\circ = \arcsin\left(\frac{29 \text{ kg} \cdot 9.8066 \text{ m/s}^2 - 29 \text{ kg} \cdot 5.94 \text{ m/s}^2 - 13.52 \text{ kg} \cdot 5.94 \text{ m/s}^2}{13.52 \text{ kg} \cdot 9.8066 \text{ m/s}^2}\right)$$

### 4.3) Angle of Inclination given Tension Formula

[Evaluate Formula !\[\]\(21199eb166cc97331a0c54c649195dcc\_img.jpg\)](#)**Formula**

$$\theta_p = \arcsin\left(\frac{T \cdot (m_1 + m_2)}{m_1 \cdot m_2 \cdot [g]} - 1\right)$$

**Example with Units**

$$13.23^\circ = \arcsin\left(\frac{111.1232 \text{ N} \cdot (29 \text{ kg} + 13.52 \text{ kg})}{29 \text{ kg} \cdot 13.52 \text{ kg} \cdot 9.8066 \text{ m/s}^2} - 1\right)$$

### 4.4) Tension in String when One Body is Lying on Smooth Inclined Plane Formula

[Evaluate Formula !\[\]\(ec9132f1d27c8919987d92907322654d\_img.jpg\)](#)**Formula**

$$T = \frac{m_1 \cdot m_2}{m_1 + m_2} \cdot [g] \cdot (1 + \sin(\theta_p))$$

**Example with Units**

$$111.1232 \text{ N} = \frac{29 \text{ kg} \cdot 13.52 \text{ kg}}{29 \text{ kg} + 13.52 \text{ kg}} \cdot 9.8066 \text{ m/s}^2 \cdot (1 + \sin(13.23^\circ))$$



## Variables used in list of Motion in Bodies Hanging by String Formulas above

- $a_b$  Acceleration of System (Meter per Square Second)
- $a_i$  Acceleration of System in Inclined Plane (Meter per Square Second)
- $a_s$  Acceleration of Body (Meter per Square Second)
- $F_{fri}$  Force of Friction (Newton)
- $m_1$  Mass of Left Body (Kilogram)
- $m_2$  Mass of Right Body (Kilogram)
- $T$  Tension (Newton)
- $T_{fs}$  Tension in Freely Suspended String (Newton)
- $T_{st}$  Tension in String (Newton)
- $\theta_b$  Inclination of body (Degree)
- $\theta_p$  Inclination of Plane (Degree)
- $\mu_{hor}$  Coefficient of Friction for Horizontal Plane
- $\mu_{hs}$  Coefficient of Friction for Hanging String

## Constants, Functions, Measurements used in list of Motion in Bodies Hanging by String Formulas above

- **constant(s):**  $[g]$ , 9.80665  
*Gravitational acceleration on Earth*
- **Functions:** **acos**,  $\text{acos}(\text{Number})$   
*The inverse cosine function, is the inverse function of the cosine function. It is the function that takes a ratio as an input and returns the angle whose cosine is equal to that ratio.*
- **Functions:** **asin**,  $\text{asin}(\text{Number})$   
*The inverse sine function, is a trigonometric function that takes a ratio of two sides of a right triangle and outputs the angle opposite the side with the given ratio.*
- **Functions:** **cos**,  $\text{cos}(\text{Angle})$   
*Cosine of an angle is the ratio of the side adjacent to the angle to the hypotenuse of the triangle.*
- **Functions:** **sec**,  $\text{sec}(\text{Angle})$   
*Secant is a trigonometric function that is defined ratio of the hypotenuse to the shorter side adjacent to an acute angle (in a right-angled triangle); the reciprocal of a cosine.*
- **Functions:** **sin**,  $\text{sin}(\text{Angle})$   
*Sine is a trigonometric function that describes the ratio of the length of the opposite side of a right triangle to the length of the hypotenuse.*
- **Functions:** **tan**,  $\text{tan}(\text{Angle})$   
*The tangent of an angle is a trigonometric ratio of the length of the side opposite an angle to the length of the side adjacent to an angle in a right triangle.*
- **Measurement:** **Weight** in Kilogram (kg)  
*Weight Unit Conversion*
- **Measurement:** **Acceleration** in Meter per Square Second (m/s<sup>2</sup>)  
*Acceleration Unit Conversion*
- **Measurement:** **Force** in Newton (N)  
*Force Unit Conversion*
- **Measurement:** **Angle** in Degree (°)  
*Angle Unit Conversion*



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