

Important Unsymmetrical Bending and Three Hinged Arches Formulas PDF



Formulas
Examples
with Units

List of 15 Important Unsymmetrical Bending and Three Hinged Arches Formulas

1) Three Hinged Arches Formulas ↻

1.1) Angle between Horizontal and Arch Formula ↻

Formula

$$y' = f \cdot 4 \cdot \frac{1 - (2 \cdot x_{\text{Arch}})}{l^2}$$

Example with Units

$$0.5625 = 3\text{m} \cdot 4 \cdot \frac{16\text{m} - (2 \cdot 2\text{m})}{16\text{m}^2}$$

Evaluate Formula ↻

1.2) Horizontal Distance from Support to Section for Angle between Horizontal and Arch Formula ↻

Formula

$$x_{\text{Arch}} = \left(\frac{l}{2}\right) - \left(\frac{y' \cdot l^2}{8 \cdot f}\right)$$

Example with Units

$$2.6667\text{m} = \left(\frac{16\text{m}}{2}\right) - \left(\frac{0.5 \cdot 16\text{m}^2}{8 \cdot 3\text{m}}\right)$$

Evaluate Formula ↻

1.3) Ordinate at any point along Central Line of Three-hinged Parabolic Arch Formula ↻

Formula

$$y_{\text{Arch}} = \left(4 \cdot f \cdot \frac{x_{\text{Arch}}}{l^2}\right) \cdot (l - x_{\text{Arch}})$$

Example with Units

$$1.3125\text{m} = \left(4 \cdot 3\text{m} \cdot \frac{2\text{m}}{16\text{m}^2}\right) \cdot (16\text{m} - 2\text{m})$$

Evaluate Formula ↻

1.4) Ordinate of any point along Central Line of Three-hinged Circular Arch Formula ↻

Formula

$$y_{\text{Arch}} = \left(\left(R^2 - \left(\left(\frac{l}{2} - x_{\text{Arch}} \right)^2 \right)^{\frac{1}{2}} \right) \right) \cdot R + f$$

Evaluate Formula ↻

Example with Units

$$3\text{m} = \left(\left((6\text{m}^2) - \left(\left(\frac{16\text{m}}{2} - 2\text{m} \right)^2 \right)^{\frac{1}{2}} \right) \right) \cdot 6\text{m} + 3\text{m}$$



1.5) Rise of Arch in Three-hinged Circular Arch Formula

Evaluate Formula 

Formula

$$f = \left(\left(\left(R^2 \right) - \left(\left(\frac{l}{2} \right) - x_{\text{Arch}} \right)^2 \right)^{\frac{1}{2}} \right) \cdot R + y_{\text{Arch}}$$

Example with Units

$$1.4 \text{ m} = \left(\left(\left(6 \text{ m}^2 \right) - \left(\left(\frac{16 \text{ m}}{2} \right) - 2 \text{ m} \right)^2 \right)^{\frac{1}{2}} \right) \cdot 6 \text{ m} + 1.4 \text{ m}$$

1.6) Rise of Three-hinged Arch for Angle between Horizontal and Arch Formula

Formula

$$f = \frac{y' \cdot (l^2)}{4 \cdot (1 - (2 \cdot x_{\text{Arch}}))}$$

Example with Units

$$2.6667 \text{ m} = \frac{0.5 \cdot (16 \text{ m}^2)}{4 \cdot (16 \text{ m} - (2 \cdot 2 \text{ m}))}$$

Evaluate Formula 

1.7) Rise of three-hinged Parabolic Arch Formula

Formula

$$f = \frac{y_{\text{Arch}} \cdot (l^2)}{4 \cdot x_{\text{Arch}} \cdot (1 - x_{\text{Arch}})}$$

Example with Units

$$3.2 \text{ m} = \frac{1.4 \text{ m} \cdot (16 \text{ m}^2)}{4 \cdot 2 \text{ m} \cdot (16 \text{ m} - 2 \text{ m})}$$

Evaluate Formula 

1.8) Span of Arch in Three-hinged Circular Arch Formula

Evaluate Formula 

Formula

$$l = 2 \cdot \left(\left(\left(\sqrt{\left(R^2 \right) - \left(\frac{y_{\text{Arch}} - f}{R} \right)^2} \right) + x_{\text{Arch}} \right) \right)$$

Example with Units

$$15.9881 \text{ m} = 2 \cdot \left(\left(\left(\sqrt{\left(6 \text{ m}^2 \right) - \left(\frac{1.4 \text{ m} - 3 \text{ m}}{6 \text{ m}} \right)^2} \right) + 2 \text{ m} \right) \right)$$



2) Unsymmetrical Bending Formulas

2.1) Bending Moment about Axis XX given Maximum Stress in Unsymmetrical Bending Formula

Formula

$$M_x = \left(f_{\text{Max}} - \left(\frac{M_y \cdot x}{I_y} \right) \right) \cdot \frac{I_x}{y}$$

Evaluate Formula 

Example with Units

$$238.8369 \text{ N}^*\text{m} = \left(1430 \text{ N/m}^2 - \left(\frac{307 \text{ N}^*\text{m} \cdot 104 \text{ mm}}{50 \text{ kg}\cdot\text{m}^2} \right) \right) \cdot \frac{51 \text{ kg}\cdot\text{m}^2}{169 \text{ mm}}$$

2.2) Bending Moment about Axis YY given Maximum Stress in Unsymmetrical Bending Formula

Formula

$$M_y = \left(f_{\text{Max}} - \left(\frac{M_x \cdot y}{I_x} \right) \right) \cdot \frac{I_y}{x}$$

Evaluate Formula 

Example with Units

$$306.7402 \text{ N}^*\text{m} = \left(1430 \text{ N/m}^2 - \left(\frac{239 \text{ N}^*\text{m} \cdot 169 \text{ mm}}{51 \text{ kg}\cdot\text{m}^2} \right) \right) \cdot \frac{50 \text{ kg}\cdot\text{m}^2}{104 \text{ mm}}$$

2.3) Distance from Point to XX Axis given Maximum Stress in Unsymmetrical Bending Formula

Formula

$$y = \left(f_{\text{Max}} - \left(\frac{M_y \cdot x}{I_y} \right) \right) \cdot \frac{I_x}{M_x}$$

Evaluate Formula 

Example with Units

$$168.8847 \text{ mm} = \left(1430 \text{ N/m}^2 - \left(\frac{307 \text{ N}^*\text{m} \cdot 104 \text{ mm}}{50 \text{ kg}\cdot\text{m}^2} \right) \right) \cdot \frac{51 \text{ kg}\cdot\text{m}^2}{239 \text{ N}^*\text{m}}$$



2.4) Distance from YY axis to stress point given Maximum Stress in Unsymmetrical Bending Formula

Formula

$$x = \left(f_{\text{Max}} - \left(\frac{M_x \cdot y}{I_x} \right) \right) \cdot \frac{I_y}{M_y}$$

Evaluate Formula 

Example with Units

$$103.912 \text{ mm} = \left(1430 \text{ N/m}^2 - \left(\frac{239 \text{ N}^*\text{m} \cdot 169 \text{ mm}}{51 \text{ kg}\cdot\text{m}^2} \right) \right) \cdot \frac{50 \text{ kg}\cdot\text{m}^2}{307 \text{ N}^*\text{m}}$$

2.5) Maximum Stress in Unsymmetrical Bending Formula

Formula

$$f_{\text{Max}} = \left(\frac{M_x \cdot y}{I_x} \right) + \left(\frac{M_y \cdot x}{I_y} \right)$$

Evaluate Formula 

Example with Units

$$1430.5404 \text{ N/m}^2 = \left(\frac{239 \text{ N}^*\text{m} \cdot 169 \text{ mm}}{51 \text{ kg}\cdot\text{m}^2} \right) + \left(\frac{307 \text{ N}^*\text{m} \cdot 104 \text{ mm}}{50 \text{ kg}\cdot\text{m}^2} \right)$$

2.6) Moment of Inertia about XX given Maximum Stress in Unsymmetrical Bending Formula

Formula

$$I_x = \frac{M_x \cdot y}{f_{\text{Max}} - \left(\frac{M_y \cdot x}{I_y} \right)}$$

Example with Units

$$51.0348 \text{ kg}\cdot\text{m}^2 = \frac{239 \text{ N}^*\text{m} \cdot 169 \text{ mm}}{1430 \text{ N/m}^2 - \left(\frac{307 \text{ N}^*\text{m} \cdot 104 \text{ mm}}{50 \text{ kg}\cdot\text{m}^2} \right)}$$

Evaluate Formula 

2.7) Moment of Inertia about YY given Maximum Stress in Unsymmetrical Bending Formula

Formula

$$I_y = \frac{M_y \cdot x}{f_{\text{Max}} - \left(\frac{M_x \cdot y}{I_x} \right)}$$

Example with Units

$$50.0423 \text{ kg}\cdot\text{m}^2 = \frac{307 \text{ N}^*\text{m} \cdot 104 \text{ mm}}{1430 \text{ N/m}^2 - \left(\frac{239 \text{ N}^*\text{m} \cdot 169 \text{ mm}}{51 \text{ kg}\cdot\text{m}^2} \right)}$$





Evaluate Formula 



Variables used in list of Unsymmetrical Bending and Three Hinged Arches Formulas above



- **f** Rise of arch (Meter)
- **f_{Max}** Maximum Stress (Newton per Square Meter)
- **I_x** Moment of Inertia about X-Axis (Kilogram Square Meter)
- **I_y** Moment of Inertia about Y-Axis (Kilogram Square Meter)
- **l** Span of Arch (Meter)
- **M_x** Bending Moment about X-Axis (Newton Meter)
- **M_y** Bending Moment about Y-Axis (Newton Meter)
- **R** Radius of Arch (Meter)
- **x** Distance from Point to YY Axis (Millimeter)
- **x_{Arch}** Horizontal Distance from Support (Meter)
- **y** Distance from Point to XX Axis (Millimeter)
- **y'** Angle between Horizontal and Arch
- **y_{Arch}** Ordinate of Point on Arch (Meter)

Constants, Functions, Measurements used in list of Unsymmetrical Bending and Three Hinged Arches Formulas above

- **Functions: sqrt**, sqrt(Number)
A square root function is a function that takes a non-negative number as an input and returns the square root of the given input number.
- **Measurement: Length** in Meter (m), Millimeter (mm)
Length Unit Conversion 
- **Measurement: Pressure** in Newton per Square Meter (N/m²)
Pressure Unit Conversion 
- **Measurement: Moment of Inertia** in Kilogram Square Meter (kg·m²)
Moment of Inertia Unit Conversion 
- **Measurement: Moment of Force** in Newton Meter (N*m)
Moment of Force Unit Conversion 



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