

Important Design for Beams and Ultimate Strength for Rectangular Beams with Tension Reinforcement Formulas PDF



Formulas
Examples
with Units

List of 16 Important Design for Beams and Ultimate Strength for Rectangular Beams with Tension Reinforcement Formulas

1) Bond and Anchorage for Reinforcing Bars Formulas

1.1) Beam Effective Depth given Bond Stress on Bar Surface Formula

Formula

$$d_{\text{eff}} = \frac{\Sigma S}{j \cdot u \cdot \text{Summation}_0}$$

Example with Units

$$3.996\text{m} = \frac{320\text{N}}{0.8 \cdot 10\text{N/m}^2 \cdot 10.01\text{m}}$$

Evaluate Formula

1.2) Bond Stress on Bar Surface Formula

Formula

$$u = \frac{\Sigma S}{j \cdot d_{\text{eff}} \cdot \text{Summation}_0}$$

Example with Units

$$9.99\text{N/m}^2 = \frac{320\text{N}}{0.8 \cdot 4\text{m} \cdot 10.01\text{m}}$$

Evaluate Formula

1.3) Tensile Reinforcing Bars Perimeters Sum given Bond Stress on Bar Surface Formula

Formula

$$\text{Summation}_0 = \frac{\Sigma S}{j \cdot d_{\text{eff}} \cdot u}$$

Example with Units

$$10\text{m} = \frac{320\text{N}}{0.8 \cdot 4\text{m} \cdot 10\text{N/m}^2}$$

Evaluate Formula

1.4) Total Shear given Bond Stress on Bar Surface Formula

Formula

$$\Sigma S = u \cdot (j \cdot d_{\text{eff}} \cdot \text{Summation}_0)$$

Example with Units

$$320.32\text{N} = 10\text{N/m}^2 \cdot (0.8 \cdot 4\text{m} \cdot 10.01\text{m})$$

Evaluate Formula

2) Shear Reinforcement Formulas

2.1) 28 Day Concrete Compressive Strength given Development Length for Hooked Bar Formula

Formula

$$f_c = \left(\frac{1200 \cdot D_b}{L_d} \right)^2$$

Example with Units

$$15.0001\text{MPa} = \left(\frac{1200 \cdot 1.291\text{m}}{400\text{mm}} \right)^2$$

Evaluate Formula



2.2) Area of Steel Required in Vertical Stirrups Formula

Formula

$$A_s = \frac{V_s \cdot s}{f_{y\text{steel}} \cdot D_{\text{centroid}}}$$

Example with Units

$$0.3929\text{mm}^2 = \frac{100\text{MPa} \cdot 50.1\text{mm}}{250\text{MPa} \cdot 51.01\text{mm}}$$

Evaluate Formula 

2.3) Bar Diameter given Development Length for Hooked Bar Formula

Formula

$$D_b = \frac{(L_d) \cdot \left(\sqrt{f_c}\right)}{1200}$$

Example with Units

$$1.291\text{m} = \frac{(400\text{mm}) \cdot \left(\sqrt{15\text{MPa}}\right)}{1200}$$

Evaluate Formula 

2.4) Development Length for Hooked Bar Formula

Formula

$$L_d = \frac{1200 \cdot D_b}{\sqrt{f_c}}$$

Example with Units

$$400.0017\text{mm} = \frac{1200 \cdot 1.291\text{m}}{\sqrt{15\text{MPa}}}$$

Evaluate Formula 

2.5) Nominal Reinforcement Shear Strength for Stirrup Area with Support Angle Formula

Formula

$$V_s = A_v \cdot f_{y\text{steel}} \cdot \sin(\alpha)$$

Example with Units

$$62500\text{MPa} = 500\text{mm}^2 \cdot 250\text{MPa} \cdot \sin(30^\circ)$$

Evaluate Formula 

2.6) Nominal Shear Strength of Concrete Formula

Formula

$$V_c = \left(1.9 \cdot \sqrt{f_c} + \left((2500 \cdot \rho_w) \cdot \left(\frac{V_u \cdot D_{\text{centroid}}}{B_M} \right) \right) \right) \cdot (b_w \cdot D_{\text{centroid}})$$

Example with Units

$$71.3871\text{MPa} = \left(1.9 \cdot \sqrt{15\text{MPa}} + \left((2500 \cdot 0.08) \cdot \left(\frac{100.1\text{kN} \cdot 51.01\text{mm}}{49.5\text{kN}\cdot\text{m}} \right) \right) \right) \cdot (50.00011\text{mm} \cdot 51.01\text{mm})$$

Evaluate Formula 

2.7) Nominal Shear Strength Provided by Reinforcement Formula

Formula

$$V_s = V_n - V_c$$

Example with Units

$$100\text{MPa} = 190\text{MPa} - 90\text{MPa}$$

Evaluate Formula 



2.8) Stirrup Area given Stirrup Spacing in Practical Design Formula

Formula

$$A_v = (s) \cdot \frac{V_u - \left(2 \cdot \Phi \cdot \sqrt{f_c} \cdot d_{eff} \cdot b_w \right)}{\Phi \cdot f_y \cdot d_{eff}}$$

Evaluate Formula 

Example with Units

$$2119.7275 \text{ mm}^2 = (50.1 \text{ mm}) \cdot \frac{1275 \text{ kN} - \left(2 \cdot 0.75 \cdot \sqrt{15 \text{ MPa}} \cdot 4 \text{ m} \cdot 300 \text{ mm} \right)}{0.75 \cdot 9.99 \text{ MPa} \cdot 4 \text{ m}}$$

2.9) Stirrup Area given Support Angle Formula

Formula

$$A_v = \frac{V_s}{f_y} \cdot \sin(\alpha)$$

Example with Units

$$10010.01 \text{ mm}^2 = \frac{200 \text{ kN}}{9.99 \text{ MPa}} \cdot \sin(30^\circ)$$

Evaluate Formula 

2.10) Stirrup Spacing for Practical Design Formula

Formula

$$s = \frac{A_v \cdot \Phi \cdot f_{y_{steel}} \cdot d_{eff}}{(V_u) - \left((2 \cdot \Phi) \cdot \sqrt{f_c} \cdot b_w \cdot d_{eff} \right)}$$

Evaluate Formula 

Example with Units

$$295.7346 \text{ mm} = \frac{500 \text{ mm}^2 \cdot 0.75 \cdot 250 \text{ MPa} \cdot 4 \text{ m}}{(1275 \text{ kN}) - \left((2 \cdot 0.75) \cdot \sqrt{15 \text{ MPa}} \cdot 300 \text{ mm} \cdot 4 \text{ m} \right)}$$

2.11) Stirrups area for Inclined Stirrups Formula

Formula

$$A_v = \frac{V_s \cdot s}{(\sin(\alpha) + \cos(\alpha)) \cdot f_y \cdot d_{eff}}$$

Evaluate Formula 

Example with Units

$$183.5623 \text{ mm}^2 = \frac{200 \text{ kN} \cdot 50.1 \text{ mm}}{(\sin(30^\circ) + \cos(30^\circ)) \cdot 9.99 \text{ MPa} \cdot 4 \text{ m}}$$



2.12) Ultimate Shear Capacity of Beam Section Formula

Formula

$$V_n = (V_c + V_s)$$

Example with Units

$$190 \text{ MPa} = (90 \text{ MPa} + 100 \text{ MPa})$$








Evaluate Formula 



Variables used in list of Design for Beams and Ultimate Strength for Rectangular Beams with Tension Reinforcement Formulas above

- **A_s** Area of Steel required (Square Millimeter)
- **A_v** Stirrup Area (Square Millimeter)
- **B_M** Bending Moment of Considered Section (Kilonewton Meter)
- **b_w** Width of Beam Web (Millimeter)
- **bw** Breadth of Web (Millimeter)
- **D_b** Bar Diameter (Meter)
- **D_{centroid}** Centroidal Distance of Tension Reinforcement (Millimeter)
- **d_{eff}** Effective Depth of Beam (Meter)
- **f_c** 28 Day Compressive Strength of Concrete (Megapascal)
- **f_y** Yield Strength of Reinforcement (Megapascal)
- **$f_{y\text{steel}}$** Yield Strength of Steel (Megapascal)
- **j** Constant j
- **L_d** Development Length (Millimeter)
- **s** Stirrup Spacing (Millimeter)
- **Summation_0** Perimeter Sum of Tensile Bars (Meter)
- **u** Bond Stress on Surface of Bar (Newton per Square Meter)
- **V_c** Nominal Shear Strength of Concrete (Megapascal)
- **V_n** Ultimate Shear Capacity (Megapascal)
- **V_s** Nominal Shear Strength by Reinforcement (Megapascal)
- **V_u** Shear Force in considered Section (Kilonewton)
- **V_s** Strength of Shear Reinforcement (Kilonewton)
- **V_u** Design of Shear Stress (Kilonewton)
- **α** Angle at which Stirrup is inclined (Degree)
- **ρ_w** Reinforcement Ratio of Web Section
- **ΣS** Total Shear Force (Newton)

Constants, Functions, Measurements used in list of Design for Beams and Ultimate Strength for Rectangular Beams with Tension Reinforcement Formulas above




- **Functions:** **cos**, cos(Angle)
Cosine of an angle is the ratio of the side adjacent to the angle to the hypotenuse of the triangle.
- **Functions:** **sin**, sin(Angle)
Sine is a trigonometric function that describes the ratio of the length of the opposite side of a right triangle to the length of the hypotenuse.
- **Functions:** **sqrt**, sqrt(Number)
A square root function is a function that takes a non-negative number as an input and returns the square root of the given input number.
- **Measurement:** **Length** in Meter (m), Millimeter (mm)
Length Unit Conversion 
- **Measurement:** **Area** in Square Millimeter (mm²)
Area Unit Conversion 
- **Measurement:** **Pressure** in Newton per Square Meter (N/m²), Megapascal (MPa)
Pressure Unit Conversion 
- **Measurement:** **Force** in Newton (N), Kilonewton (kN)
Force Unit Conversion 
- **Measurement:** **Angle** in Degree (°)
Angle Unit Conversion 
- **Measurement:** **Moment of Force** in Kilonewton Meter (kN*m)
Moment of Force Unit Conversion 
- **Measurement:** **Stress** in Megapascal (MPa)
Stress Unit Conversion 









- Φ Capacity Reduction Factor



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